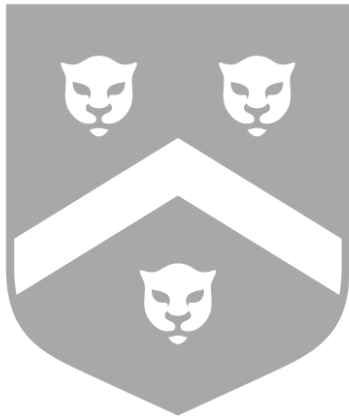


Intro to Programming Languages



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A First Look at F#

Motivation
Functional Languages
F#
Running F# in IDE
1+2*3

The F#
language

F# Types

A First Look at F#

Why F#?

- 1 Very high level above machine architecture — powerful
- 2 Functional language — everything returns a result
- 3 Interactive — code and test immediately
- 4 Minimal side effects – easier to reason about program behavior
- 5 Object-oriented
- 6 Pattern matching programming style
- 7 Useful for studying fundamentals of languages
- 8 F# runs on the .NET CLR.
- 9 C# and F# classes can be freely mixed.

Functional Languages

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1+2*3

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Example (a factorial function in F#)

```
let rec factorial x =  
    if x <= 0 then 1 else x * factorial (x-1);;
```

- Hallmarks of functional languages:
 - Single-valued variables
 - Heavy use of recursion
 - Functions are first-class citizens, can be used as parameters, function results, etc.
 - Minimal use of assignments and side-effects

F#

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at F#

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1+2*3

The F#
language

F# Types

- Open standard adopted/supported by Microsoft
- Created as an implementation of OCaml
- Full support for functional programming
- Very strong static type system
- Useful in Artificial Intelligence and programming languages
- Compatible with .NET
- Object oriented

- In lab this week: Download IDE installers from course website
- Enter F# instructions into the Read Eval Print Loop (REPL)
 - `dotnet fsi` on Linux/OS X
 - `fsi` on Windows
- F# has two running modes with slightly different syntax
 - **interactive mode:** `;;` at the end of expressions
 - **source code:** no `;;` at the end of expressions
- Lecture examples will always use interactive formatting
- Lecture examples also include ‘>’ prompt character, which should not be typed as part of an expression


$$1 + 2 \times 3$$

Example

```
> 1+2*3;;  
val it : int = 7
```

- Type an expression after > prompt; F# replies with value and type
- Variable **it** is a variable with the returned result.
- Notice F# inferred the type as int.

The F# language

Number constants

A First Look
at F#

The F#
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Constants

Number constants

bool constants

char and string

Operators

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F# Types

Example

```
> 1234;;  
val it : int = 1234  
> 123.4;;  
val it : float = 123.4
```

- Integer constants: standard decimal
- Float constants: standard decimal notation
- Note the type names: **int**, **float**

bool constants

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```
> true;;  
val it : bool = true  
> false;;  
val it : bool = false
```

- bool constants **true** and **false**
- F# is case-sensitive: use **true**, not **True** or **TRUE**
- Note type name: **bool**

char and string constants

Example

```
> "fred";  
val it : string = "fred"  
> "H";;  
val it : string = "H"  
> 'H';;  
val it : char = 'H'
```

- String constants: text inside double quotes
- Can use C-style escapes: `\n`, `\t`, `\`, `\'`, etc.
- Character constants: 1 character inside single quotes
- Note type names: **string** and **char**

Arithmetic

A First Look
at F#

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More Relations

bool operators

Short-circuiting

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Example

```
> -1 + 2 - 3 * 4 / 5 % 6;;
```

```
val it : int = -1
```

```
> -1.0 + 2.0 - 3.0 * 4.0 / 5.0;;
```

```
val it : float = -1.4
```

- Standard operators for integers, using $-$ for unary negation and for binary subtraction
- Same operators for floats
- Left associative, precedence is $\{+, -\} < \{*, /, \%\} < \{-\}$.

Concatenation and Relations

Example

```
> "bibity" + "bobity" + "boo";;  
val it : string = "bibitybobityboo"  
> 2 < 3;;  
val it : bool = true  
> 1.0 <= 1.0;;  
val it : bool = true  
> 'd' > 'c';;  
val it : bool = true  
> "abce" >= "abd";;  
val it : bool = false
```

- String concatenation: + operator
- Ordering comparisons: <, >, <=, >=, apply to all types so far: these are *comparable types*

More Relations

Example

```
> 1=2;;  
val it : bool = false  
> 1 = 2;;  
val it : bool = false  
> true <> false;;  
val it : bool = true  
> 1.3 = 1.3;;  
val it : bool = true  
> [1; 4; 6] = [1; 4; 6];;  
val it : bool = true
```

- Equality comparisons: = and <>
- Most types are equality testable: these are *equality types*

bool operators

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Example

```
> 1 < 1 + 1 || 3 > 4;;  
val it : bool = true  
> 1 < 2 && not (3 < 4);;  
val it : bool = false
```

- bool operators: **&&**, **||**, **not**. (And we can also use **=** for equivalence and **<>** for exclusive or.)
- Precedence so far: $\{||\} < \{\&\&\} < \{=, <>, <, >, <=, >=\}$
 $\} < \{+, -\} < \{*, /, \%\} < \{-, \mathbf{not}\}$

Short-circuiting bool operations

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Example

```
> true || 1 / 0 = 0;;  
val it : bool = true
```

Note: `&&` and `||` are short-circuiting operators: if the first operand of `||` is true, the second is not evaluated; likewise if the first operand of `&&` is false.

Conditionals

Example

```
> if (1 < 2) then "1 < 2" else "2 < 1";;  
val it : string = "1 < 2"  
> if (1 > 2) then 34 else 56;;  
val it : int = 56  
> 1 + (if (1 < 2) then 34 else 56);;  
val it : int = 35
```

- Value of the expression is the value of the **true** part if the test part is true or the value of the **else** part otherwise
- **if...** construct throws an error, result type cannot be determined

Conditional errors

Example

```
> if (true) then 1.0 else 'a';;  
error FS0001: All branches of an 'if' expression  
must return values implicitly convertible to  
the type of the first branch, which here is  
'float'. This branch returns a value of  
type 'char'.
```

```
> if (false) then "OK" else 1.0;;  
error FS0001: <clipped error>
```

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What is the value and F# type for each expression?

- 1 `"abc" + "def" + "gh";;`
- 2 `if (1 < 2) then 3.0 else 4.0;;`
- 3 `5 * (if (1 < 2) then 3 else 4);;`
- 4 `1 < 2 || (1 / 0) == 0;;`
- 5 `if (3 < 4) then 5;;`
- 6 `if (3 > 4) then 5 else 0;;`
- 7 `if (3 > 4) then 2 else '2';;`

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Implicit type conversion

Example

```
> 1 * 2;;
val it : int = 2
> 1.0 * 2;;
error FS0001: The type 'int' does not match the
type 'float'
> 1.0 < 2;;
val it: bool = true
```

- The `*`, `+` and other arithmetic operators are overloaded to have one meaning on pairs of ints, and another on pairs of floats.
- F# **does not** perform implicit type conversion with one important exception:
 - `int32` \rightarrow `double`

Explicit type conversion

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Example

```
> float 123;;  
val it : float = 123.0  
> (float 123) * 2.0;;  
val it: float = 246.0  
> floor 3.6;;  
val it : float = 3.0  
> (floor 3.6) < 4.0;;  
val it : bool = true  
> float "123";;  
val it : float = 123.0
```

Exercises

What is the result for each expression?

- 1 `floor 5;;`
- 2 `ceil 5.5;;`
- 3 `5+4.0;;`
- 4 `if (0) then 1 else 2;;`
- 5 `if (true) then 1 else 2.0;;`
- 6 `string 97.34;;`
- 7 `97.34 + "2";;`
- 8 `97.34 + '2';;`

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Variable definition

Example

```
> let x = 1+2*3;;  
val x : int = 7  
> x;;  
val it : int = 7  
> let y = if (x = 7) then 1.0 else 2.0;;  
val y : float = 1.0
```

- Define a new variable and bind to a value using **let**.
- Variable names should consist of a letter, followed by zero or more letters, digits, and/or underscores (or most things surrounded with ``).

Multiple variable definitions

Example

```
> let x = 23;;  
val x : int = 23  
> let x = true;;  
val x : bool = true  
> x = 23;;  
error FS0001: This expression was expected to  
have type 'bool' but here has type 'int'
```

- Can define a new variable with the same name as an old one, even using a different type. (This is not particularly useful.)
- This is not the same as assignment. It defines a new variable but **does not** change the old one. Any part of the program that was using the first definition of **x**, still uses the first definition after the second definition is made.

Variable definition

Example

```
> let fred = 23;;  
val fred : int = 23  
> fred <- fred + 1;;  
error FS0027: This value is not mutable...  
> let mutable fred = 23;;  
val mutable fred : int = 23  
> fred <- fred + 1;;  
val it : unit = ()  
> fred;;  
val it : int = 24
```

- Assignment: Variables can change value using *side effects*.
- In functional programming, side effects, (e.g. assignments) are avoided.

Exercises

Suppose we make these F# declarations

- `let a = "123";;`
- `let b = "456";;`
- `let c = a + b + "789";;`
- `let a = 3 + 4;;`

What is the value and type of each of these expressions?

- `a;;`
- `b;;`
- `c;;`
- `a = 6;;`

Garbage Collection

A First Look
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Variable definition

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Garbage Collection

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- F# runs under Common Language Runtime – the VM for .NET programs
- Garbage collection responsibility of CLR
- Reclaiming pieces of memory that are no longer being used
- We'll see much more about this when we look at C#.

Tuples

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Example

```
> let barney = (1+2, 3.0*4.0, "hi");;  
val barney : int * float * string = (3, 12.0, "hi")  
> let pt1 = ("red", (30, 20));;  
val pt1 : string * (int * int) = ("red", (30, 20))  
> fst pt1;;  
val it : string = "red"  
> fst (snd pt1);;  
val it : int = 30
```

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- *Heterogeneous*: tuples can contain mixed types
- Parentheses define tuples
- A tuple is similar to a struct in C++ but with no field names
- **fst** **x** is the first element of 2-tuple **x**, **snd** **x** is the second.

Example

```
> snd ("red", 50);;  
val it : int = 50
```

No Tuple of 1

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Example

```
> (5, 6);;  
val it : int * int = (5, 6)  
> (5);;  
val it : int = 5  
> fst (5, 6);;  
val it : int = 5  
> fst (5);;  
error FS0001: This expression was expected  
to have type 'a * 'b' but here has type  
'int'
```

Tuple Type Constructor

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- The type of a tuple gives (,) as a type constructor
- For tuple `(5,true);;`, `int * bool` is the type of pairs (x, y) where x is an **int** and y is a **bool**
- Parentheses have structural significance, each below are different:
 - `(int, (int, bool)):(5,(6, true))`
 - `((int, int), string):((5,6), "Hi")`
 - `(int, int, bool):(5, 6, true)`
 - `((bool, int), (int, float)):((true,4),(5,3.1))`

Exercises

What is the result for each expression?

- 1 `snd (3, 4);;`
- 2 `let x = (1+2, 3.0*0.5, "zig" + "zag");;`
- 3 `x;;`
- 4 `(4, 5) = (4, 5);;`
- 5 `snd (3, 4, 5);;`
- 6 `(4, "zig") = (4, 5);;`
- 7 `(4, 5.0) = (4, 5);;`
- 8 `(3, "zig", 5.3);;`
- 9 `(3, (4, "zig"), 5.3);;`

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Example

```
> [1; 2; 3];;  
val it : int list = [1; 2; 3]  
> [1.0; 2.0];;  
val it : float list = [1.0; 2.0]  
> [1.0; "Hello"];;  
error FS0001: <error>  
> [[1; 2; 3]; [1; 2]];;  
val it : int list list = [[1; 2; 3]; [1; 2]]
```

- *Homogeneous*: all list elements must be the same type.
- Mixing types results in an exception

Empty Lists

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Example

```
> [];;  
val it : 'a list = []  
> let empty = [];;  
val empty : 'a list  
> empty = [];;  
val it : bool = true
```

- Empty list is []
- **List.empty** is an *alias* for []
- 'a list means a list of elements, type 'a

List Type Constructor

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- The type **list** is type constructor
- For example, in `[5;6]` the type **int list** means each element is of type `int`
- A list is not a tuple: `[5;6;7]` is not `(5,6,7)`

IsEmpty

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Example

```
> [].IsEmpty;;  
val it : bool = true  
> [1;2;3].IsEmpty;;  
val it : bool = false
```

- **IsEmpty** tests for the empty list
- Can also use an equality test, as in `x = []`

@ Operator

Example

```
> [1;2;3] @ [4;5;6];;  
val it : int list = [1; 2; 3; 4; 5; 6]
```

- @ operator concatenates two lists
- Both operands must be lists
- Both lists must have the same type

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Example

```
> let n = 5::[6;7];;  
val n : int list = [5; 6; 7]  
> let x = 5::[];;  
val x : int list = [5]  
> let y = 6::x;;  
val y : int list = [6; 5]  
> let y = 5::6::7::[];;  
val y : int list = [5; 6; 7]
```

- :: operator is a list-builder (pronounced **cons**) for *constructor*
- Constructs a new list by prepending an element to a list
- :: operator is right-associative

Head and Tail functions

Example

```
> let z = 1::2::[];;  
val z : int list = [1; 2]  
> z.Head;;  
val it : int = 1  
> z.Tail;;  
val it : int list = [2]  
> z.Tail.Tail;;  
val it : int list = []
```

- The **Head** function returns the head of a list: the first element
- The **Tail** function returns the list tail: the *list* without the Head element

Exercises

What is the result for each expression?

- `[1;2] @ [3;4];;`
- `1::2::[];;`
- `[1::2::[]];;`
- `(1::2::[]).Head;;`
- `[[1;2];[3;4]];;`
- `[[1;2];[3;4]].Tail;;`
- `[5].tail;;`
- `(snd ([1;2], [3;4])).Tail.Head;;`
- `[(3,4), (5,6)].Head;;`
- `[1;3;4].Head::2::[1;3;4].Tail;;`

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What is the result for each expression?

1 `[] .Head;;`

2 `[] .tail;;`

3 `[1;2] .Tail.Tail.Head;;`

4 `1 @ [2];;`

5 `[1] :: [2;3];;`

6 `1 :: 2 :: [] .Head;;`

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Implement each expression in F#

- 1 Concatenate [1;2] with [3;4].
- 2 1 cons'ed to [2;3].
- 3 Second element of [1;2;3;4].
- 4 Last element of [1;2;3;4].
- 5 2 cons'ed to [1;3] to yield [1;2;3].

Defining Functions

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Defining Functions

let keyword

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F# Types

Example

```
> let add x y = x + y;;  
val add : x:int -> y:int -> int
```

- **add** – the function name
- **x y** – parameter list
- **x + y** – function result
- **add : x:int -> y:int -> int** – inferred function result type

Example (C/C++/Java equivalent)

```
int add(int x, int y)  
{ return x + y; }
```

let keyword

Example

```
> let first (x: (int * string)):int = fst x;;  
val first : int * string -> int  
> first (2, "abc");;  
val it : int = 2
```

- **let** defines a new function and binds to variable **first**
- **first** is an **int * string -> int** function whose argument **x** type is **int * string** and the return type is **int**
- It is not necessary to declare any return types, since F# infers them.

Function Definition Syntax

Definition

```
<fun-def> ::=  
    let <function-name> (<parameter>:type):type =  
        <expression> ;;
```

- `<function-name>` can be any legal F# name
- The simplest `<parameter>` is just a single variable name: the formal parameter of the function
- The `<expression>` is any F# expression; its value is the value the function returns
- This is not the full F# function declaration... more later

Function Type Constructor

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- F# gives the type of functions using `->` as a type constructor
- For example, **`int -> float`** is the type of a function that takes an **`int`** parameter (the *domain* type) and produces a **`float`** result (the *range* type)
- From math: a function *maps* domain values (inputs) to range values (outputs).
- `let f (x:int):float = float (x % 4);;` maps the domain of all integers to the float range of `[0.0..3.0]`.
- The type is: `f:int -> float`

Parameter Passing

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```
> let quot (a:float) (b:float) = a / b;;  
val quot : a:float -> b:float -> float  
> quot 6.0 2.0;;  
val it : float = 3.0  
> quot 6 2;;  
val it: float = 3.0
```

- Remember: Type promotion from int to float only
- Java/C#/etc. promotes char -> int -> float

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```
> let cons a L = a::L;;  
val cons : a:'a -> L:'a list -> 'a list
```

- Function name: cons
- Parameter tuple: 'a, list of 'a
- Element one, type unknown: 'a
- Element two, list of type unknown: list of 'a
- Result list type unknown: list of 'a

Exercises

What is the result for each function call?

- `let fa (x:int) = x + 1;;`
- `fa 3;;`
- `let fb (x:'a) (y:'b) = x;;`
- `fb [1;2;3] 4;;`
- `fb 3 4;;`
- `let fc (x:'a list) = x.Tail;;`
- `fc [1; 2; 3];;`
- `let fd (x:'a list) (y:'a list) =
x.Head::y.Tail;;`
- `fd [1;2;3] [4;5;6];;`
- `let fe (x:int list) = x.Head + 1;;`
- `fe [3;2;1];;`

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What is the return type for each function?

- `let fa (x:int) = x + 1;;`
- `let fb (x:'a) (y:'b) = x;;`
- `let fc (x:'a list) = x.Tail;;`
- `let fd (x:'a list, y:'a list) = x.Head :: y.Tail;;`
- `let fe (x:int) = x.Head + 1;;`

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F# Types

- Functional languages are characterized by use of recursion for repetition
- Functional languages such as F# minimize assignment hazard of side effects
- Repetition (e.g. for, while, do while, etc.) requires assignment

Example (C++ loop)

```
for (i=0; i<10; i=i+1)
    cout << i;
```

Recursive factorial function

Example

```
> let rec fact n =  
    if (n = 0) then 1 else n * fact (n-1);;  
    // call a f'n with space-separated parameters  
val fact : n:int -> int  
> fact 5;;  
val it : int = 120
```

Many recursive functions consist of a pattern of two steps:

- Test for base case, terminating condition:
 - if (n = 0) then 1
- Recurse, moving closer to terminating condition:
 - else n * fact (n-1)

Exercises

Write the recursive functions in F#

```
int Fib( int n ) {
    if ( n <= 1 ) return n;
    else return Fib(n-1) + Fib(n-2);
}

double interest(rate, principle, year) {
    if (year == 0)
        return principle;
    else return
        interest(rate, (1.0+rate) * principle, year-1);
}
```

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Recursive int list summation

Example

```
> let rec summation (x:int list) =  
    if (x.IsEmpty) then 0  
    else x.Head + summation (x.Tail);;  
val summation : x:int list -> int  
  
> summation [1;2;3;4;5];;  
val it : int = 15
```

Common recursive function pattern for list arguments:

- base case test for empty list:
 - `if (x.isEmpty) then 0`
- recursive call moving closer to base case of `x.isEmpty`:
 - `summation(x.Tail)`

Recursive list length

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Example

```
> let rec length (x:'a list) =  
    if (x.IsEmpty) then 0  
    else 1 + length x.Tail;;  
val length : x:'a list -> int  
> length [true;false>true];;  
val it : int = 3  
> length [1;2;3];;  
val it : int = 3
```

- Function to compute the list length is predefined in F#.
- Note type `length : x:'a list -> int` works on any type of list.
- *Polymorphic*, while summation operates on int lists only.

Recursive last element in list

Example

```
> let rec last (L:'a list) =  
    if (L.Tail = []) then L.Head  
    else last L.Tail;;  
val last : L:'a list -> 'a  
> last [2;4;6;8;10];;  
val it : int = 10
```

Notice recursion pattern of:

- Test base case `L.Tail=[]`, return base case value `L.Head`
 - 1 One element remaining in `L`
 - 2 Recurse `last(L.Tail)`, moving closer to base case

Recursive n^{th} element in list

Example

```
> let rec Nth n (L:'a list) =  
    if (n = 1) then L.Head  
    else Nth (n-1) L.Tail;;  
val Nth : n:int -> L:'a list -> 'a  
> Nth 2 [true;false;true];;  
val it : bool = false  
> Nth 2 [("a", 4); ("b", -2)];;  
val it : string * int = ("b", -2)
```

- Type `n:int -> L:'a list -> 'a` works on any type of list, *polymorphic* on the list parameter.
- Fails when list has less than n elements.

Recursive list identity

Example

```
> let rec identity (L:'a list) =
    if (L.IsEmpty) then []
    else L.Head::identity(L.Tail);;
val identity : L:'a list -> 'a list
> identity [1;2;3];;
val it : int list = [1; 2; 3]
```

Notice recursion pattern of:

- Test for base case `L.IsEmpty`, return base case value `[]`
- Recurse `identity(L.Tail)`, moving closer to base case

Recursive all-but-last element

Example

```
> let rec allbutthelast (L:'a list) =  
    if (L.Tail=[]) then []  
    else L.Head::allbutthelast L.Tail;;  
val allbutthelast : L:'a list -> 'a list  
allbutthelast [1;2;3];;  
val it : int list = [1; 2]
```

Notice recursion pattern of:

- Test for base case `L.Tail=[]`, return base case value `[]`
- Recurse `allbutthelast L.Tail`, moving closer to base case

Recursive list reverse

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Example

```
> let rec reverse (L:'a list) =  
    if (L=[]) then []  
    else reverse(L.Tail)@[L.Head];;  
val reverse : L:'a list -> 'a list  
> reverse [1;2;3];;  
val it : int list = [3; 2; 1]
```

Notice recursion pattern of:

- Test for base case `L=[]`, return base case value `[]`
- Recurse `reverse(L.Tail)`, moving closer to base case



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F# Types

F# Types So Far

F# Types

F# Types So Far

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F# Types

F# Types So Far

- So far we have the primitive F# types **int**, **float**, **bool**, **char**, and **string**
- Also we have three type constructors:
 - Tuple types using (,)
 - List types using [;]
 - Function types